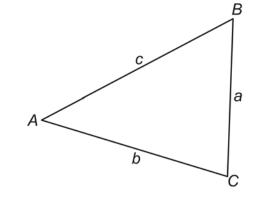
## The Law of Sines

Right triangle trigonometry can be used to solve problems involving right triangles. However, many interesting problems involve non-right triangles. In this lesson, you will use right triangle trigonometry to develop the *Law of Sines*. The law of sines is important because it can be used to solve problems involving non-right triangles as well as right triangles.

Consider oblique  $\triangle ABC$  shown to the right.

- 1. Sketch an altitude from vertex B.
- 2. Label the altitude *k*.
- 3. The altitude creates two right triangles inside  $\triangle ABC$ . Notice that  $\angle A$  is contained in one of the right triangles, and  $\angle C$  is contained in the other. Using right triangle trigonometry, write two equations, one involving sin *A*, and one involving sin *C*.

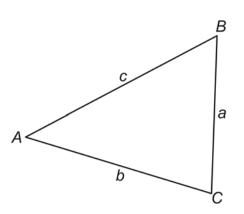
 $\sin A =$   $\sin C =$ 



- 4. Notice that each of the equations in Question 3 involves *k*. (Why does this happen?) Solve each equation for *k*.
- 5. Since both equations in Question 4 are equal to k, they can be set equal to each other. (Why is this possible?) Set the equations equal to each other to form a new equation.
- 6. Notice that the equation in Question 5 no longer involves *k*. (Why not?) Write an equation equivalent to the equation in Question 5, regrouping *a* with sin *A* and *c* with sin *C*.

Again, consider oblique  $\triangle ABC$ .

- 7. This time, sketch an altitude from vertex C.
- 8. Label the altitude *k*.
- 9. The altitude creates two right triangles inside  $\triangle ABC$ . Notice that  $\angle A$  is contained in one of the right triangles and  $\angle B$  is contained in the other. Using right triangle trigonometry, write two equations, one involving sin *A* and one involving sin *B*.



 $\sin A =$   $\sin B =$ 

- 10. Notice that each of the equations in Question 9 involves k. (Why does this happen?) Solve each equation for k.
- 11. Since both equations in Question 10 are equal to k, they can be set equal to each other. (Why is this possible?) Set the equations equal to each other to form a new equation.
- 12. Notice that the equation in Question 11 no longer involves *k*. (Why not?) Write an equation equivalent to the equation in Question 11, regrouping *a* with sin *A* and *b* with sin *B*.
- 13. Use the equations in Question 6 and Question 12 to write a third equation involving *b*, *c*, sin *B*, and sin *C*.

Together, the equations in Questions 6, 12, and 13 form the *Law of Sines*. The law of sines is important, because it can be used to solve problems involving both right and non-right triangles, because it involves only the sides and angles of a triangle.