

Good afternoon: no warm up

Assessments are being returned

HW for retakes:

GMD-A1a: p 475: #1-6,11

GMD-A1b: p 505: 3,8,10 AND p 521 #3,4,8

GMD-A2a: same as above

SRT-C7a: either practice test with this skill

SRT-C8a: video notes on applied trig

11:00- 11:55 – 1st block

12:00- 12:30 – MS Lunch/ HS DS

12:30- 1:00 – HS Lunch/ MS DS

1:05-2:00- 2nd block

2:05- 3:00- 3rd block

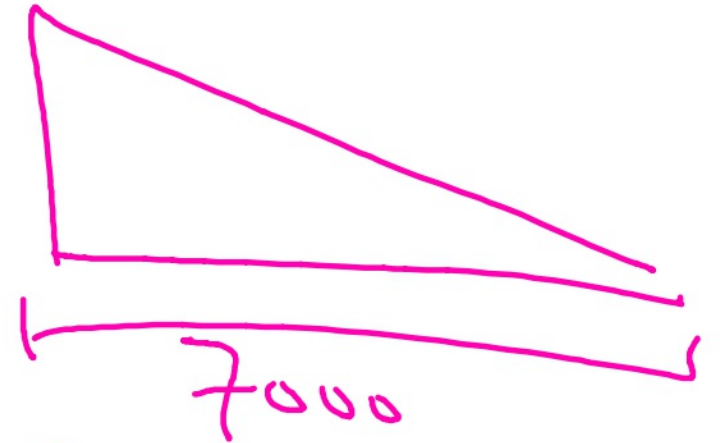
3:05-4:00- 4th block

Common Mistakes

$$\tan 31^\circ = \frac{4200}{X}$$

$$X \cdot \tan 31^\circ = 4200$$

$$X = \frac{4200}{\tan 31^\circ} \approx 7000$$



Circle circumference ✓

Circle area ✓

Cylinder volume ✓

Cylinder surface area ✓

Cone volume ✓

Cone surface area ✓

Pyramid volume ✓

Prism volume ✓

Pyramid surface area ✓

Sphere volume

Sphere surface area

Density


tested

not yet tested



Extending what we've already learned

Organizers are preparing water for an upcoming race. Each water cooler is a 2-foot tall cylinder with a 10-inch diameter. Water is distributed in cone-shaped cups 5 inches tall with a diameter of 4 inches. There are 300 runners and each runner is given 2 drinks. If each cooler costs \$35 and \$300 is budgeted for the cooler cost, calculate the amount of money left over after the coolers have been purchased.



$V_{\text{cyl}} = \pi(5)^2(24)$
 $\approx 1885 \text{ in}^3$

$V_{\text{cone}} = \frac{1}{3}(\pi)(2)^2(5)$
 $\approx 20.9 \text{ in}^3$

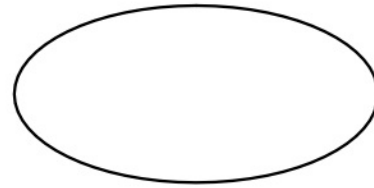
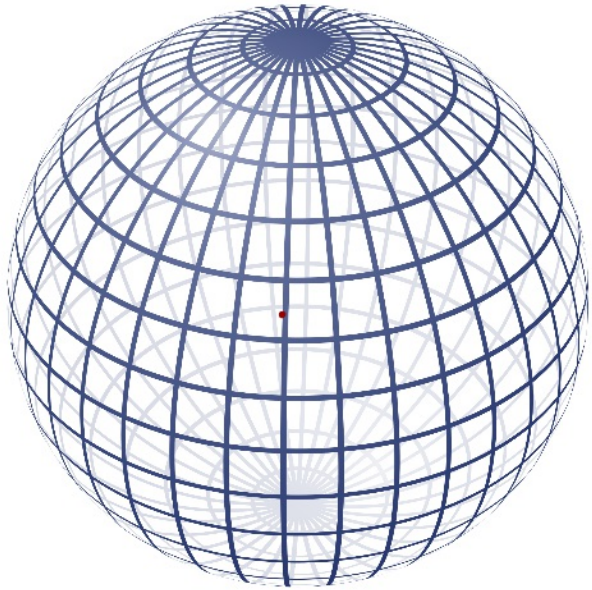
$300 = 12540 \text{ in}^3$ (total water)

$\frac{12540}{1885} = 6.66 \rightarrow 7 \text{ coolers}$

$\$300 \text{ budget} - 7 \times \$35 = \$245$

$\$55 \text{ left}$

Spheres!

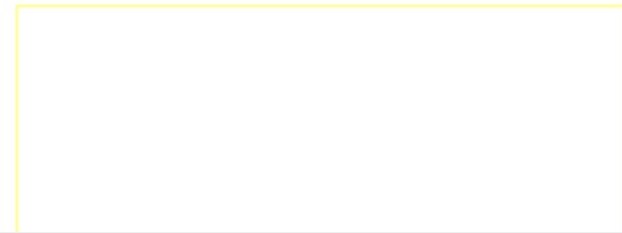
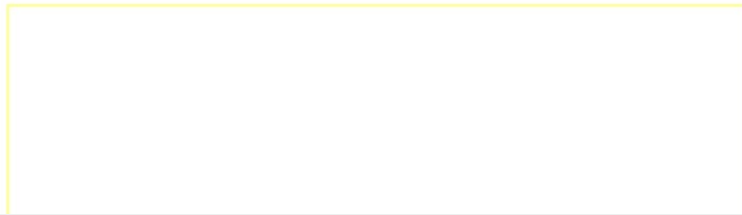


Sphere Volume

$$V = \frac{4}{3} \pi r^3$$

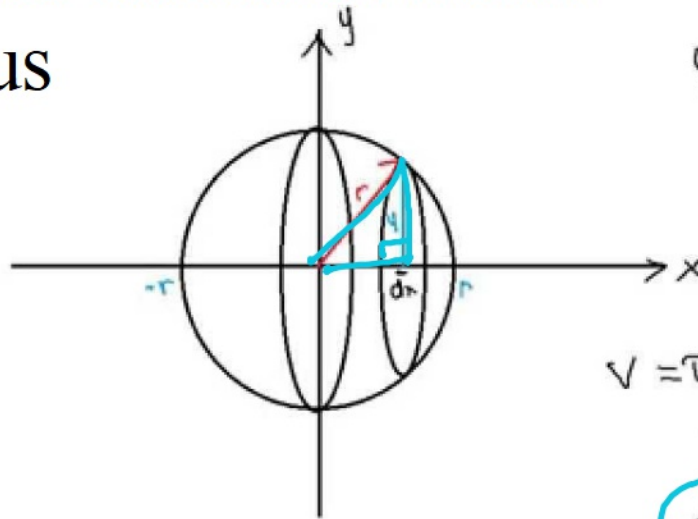
Sphere Surface Area

$$SA = 4\pi r^2$$



Why do these formulas work?

Uh...calculus



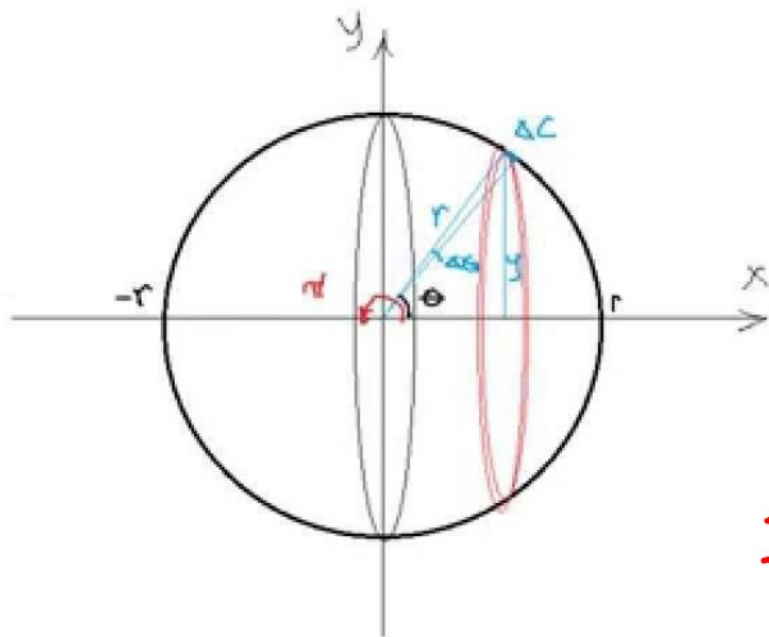
$$y^2 + x^2 = r^2$$
$$y^2 = r^2 - x^2$$

$$V = \pi \int_{-r}^r (r^2 - x^2) dx$$

$$= \pi \left[r^2 x - \frac{x^3}{3} \right]_{-r}^r$$

$$= \pi \left[\left(r^2(r) - \frac{r^3}{3} \right) - \left(r^2(-r) - \frac{(-r)^3}{3} \right) \right]$$
$$= \pi \left[r^3 - \frac{r^3}{3} \right] - \dots$$

$$A = \pi y^2$$
$$\int_0^r dV = \int_{-r}^r \pi y^2 dx$$



$$C = 2\pi y \quad y = r \sin \theta$$

$$= 2\pi r \sin \theta$$

$$\Delta A = 2\pi r \sin \theta \Delta C$$

$$\Delta C = r \Delta \theta$$

$$A = \int_0^{\pi} \underline{2\pi r \sin \theta} \cdot \underline{r} d\theta$$

$$= 2\pi r^2 \left| \underline{-\cos \theta} \right|_0^{\pi}$$

$$= 2\pi r^2 (1 + 1)$$

$$= (2\pi r^2)(2)$$

$$\underline{A = 4\pi r^2}$$

Find the exact volume of a basketball with a 12 inch diameter.



$$V = \frac{4}{3} \pi (6)^3$$

The number 4 is circled in purple. The number 6 is circled in purple and has a diagonal line through it. The number 216 is circled in purple below the 6.

$$288\pi \text{ in}^3$$

The result is enclosed in a purple rectangular box.

Now find its exact SA.

$$SA = 4\pi r^2 = 4(\pi)(6)^2$$

The number 4 is circled in red. The number 6 is circled in red and has a diagonal line through it. The number 36 is circled in red below the 6.

$$144\pi \text{ in}^2$$

The result is enclosed in a red rectangular box.

Volume

250 mL of water are frozen into slush and reshaped into a spherical snowball.

What is the approximate diameter of the snowball? (1 mL = 1 cm³)

$$V = \frac{4}{3} \pi r^3 = 250$$

$$\frac{4}{3} \pi r^3 = 250$$

$$\frac{3}{4} \left(\frac{4}{3} r^3 \right) = 79.57 \frac{3}{4}$$

$$r^3 = 59.68$$

$$r = 3.91 \text{ cm}$$

$$\frac{4}{3} r^3 = 79.5$$

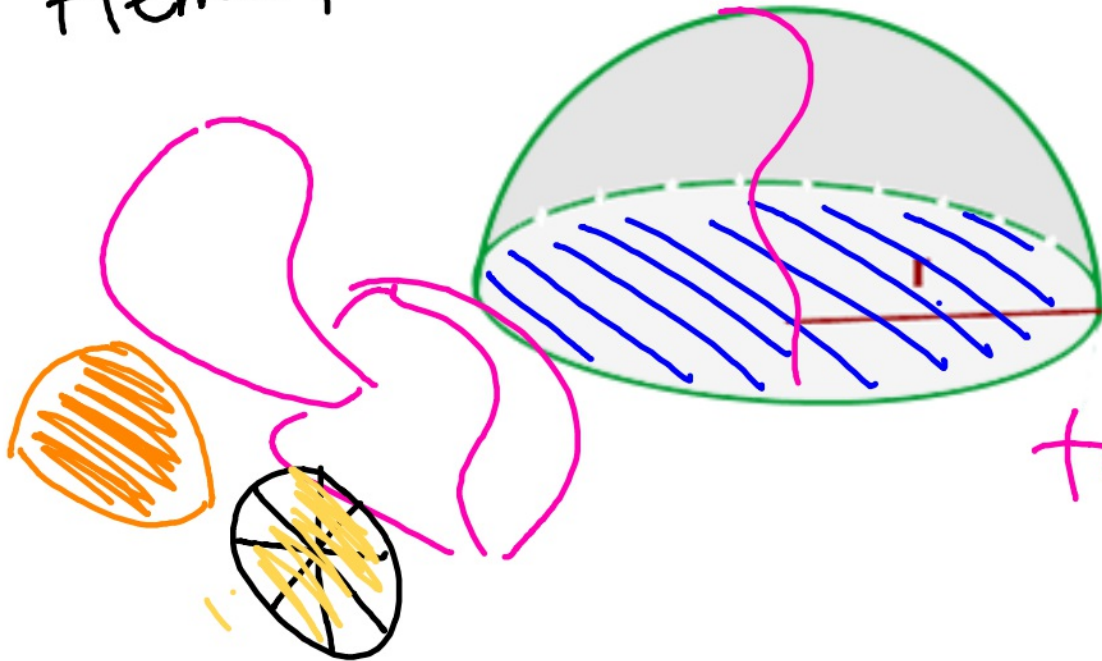
$$D = 7.82 \text{ cm}$$

use
cube
root

What would the volume be for this?

What would the surface area be for this?

Hemisphere



$$V_H = \frac{2}{3} \pi r^3$$

$$SA_H = 2 \pi r^2$$

$$\text{total } SA = 3 \pi r^2$$

HW

p. 537: #3,6, 9, 11

~~p. 522: #11-13~~

study formulas: bit.ly/formulas18