

Good morning: warm up

Find the surface area of a cone with a height of 12 and volume 100π



$$12^2 + r^2 = c^2$$

$$\underline{13 = c}$$

$$100\pi = \frac{1}{3}\pi r^2 (12)$$


$$100 = 4r^2$$

$$25 = r^2$$

$$\underline{5 = r}$$

Reminders:
test Thursday

retakes in DS (ask for a pass)

$$V_{\text{cone}} = \frac{1}{3}\pi r^2 \cdot h$$
$$SA_{\text{con}} = \pi r l + \pi r^2$$


$$SA = \pi(5)(13) + \pi(5)^2$$

$$= 65\pi + 25\pi$$

$$\underline{90\pi}$$

visibly random grouping

HW answers

505

3. $960\pi \text{ cm}^2$ (about 3016 cm^2)

8. 47.12 cm^2

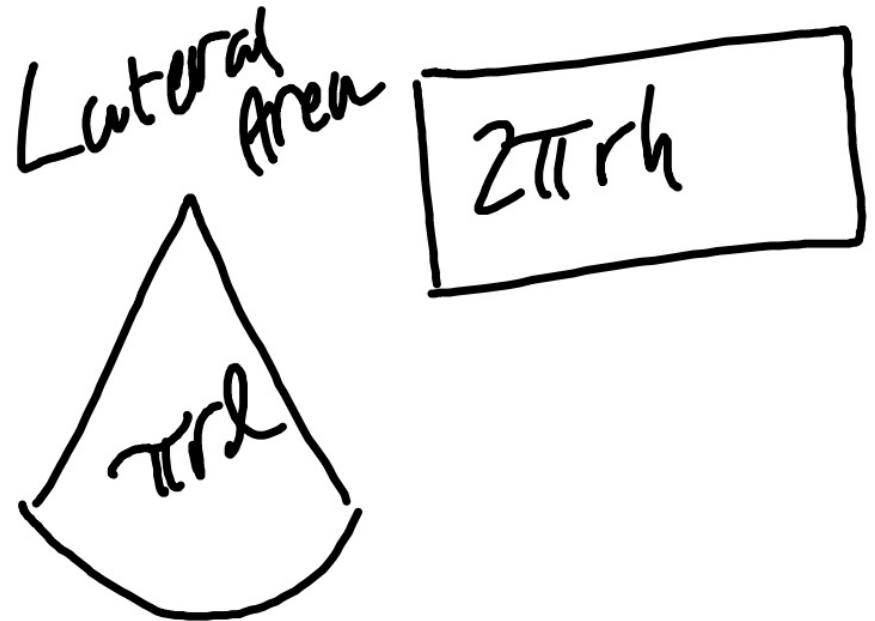
10. 6 m

521

3. LA $135\pi \text{ in}^2$, SA $216\pi \text{ in}^2$

4. a $50\pi \text{ cm}^2$ b $75\pi \text{ cm}^2$

8. 66.667 in^3



What's on Thursday's Assessment:

GMD-A1a: explain 2 of the following formulas:

circle circumference, circle area, cylinder SA, cone SA

GMD-A1b: explain 2 of the following formulas:

prism, cylinder, cone, pyramid volume

GMD-A2: use volume/SA formulas to solve a problem

SRT-C7a: sine/cosine of complements

SRT-C8a: Applied SohCahToa trig (no law of sines/cosines needed)

Brief Review of Formulas we covered:

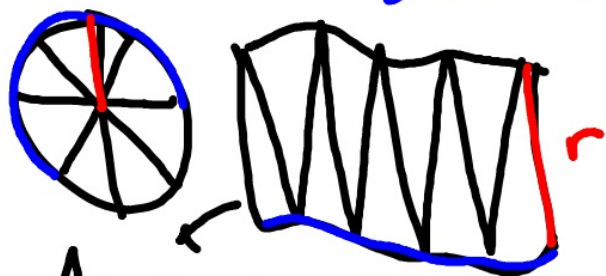
Circumference: $2\pi r$ must know the definition of $\pi = \frac{\text{Circumf.}}{\text{Diameter}}$

Circle Area: πr^2 'pizza slices, onion, octopus' method, use detailed diagrams and descriptions

Cylinder Volume: $\pi r^2 \cdot h$ stack of circles

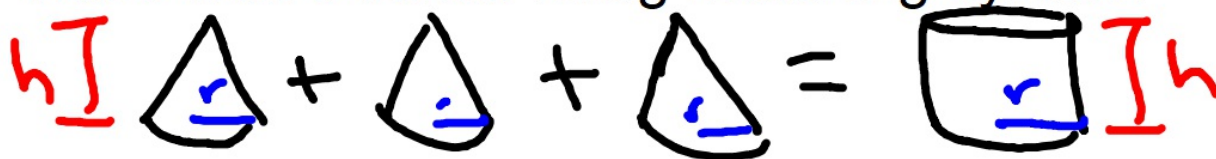
Cylinder SA: $2\pi r^2 + 2\pi rh$ rolled up rectangle, width=circumference

Cone Volume: $\frac{1}{3}\pi r^2 \cdot h$ video with 3 cones filling matching cylinder



$$A = B \cdot H$$

$$= \pi r \cdot r = \pi r^2$$

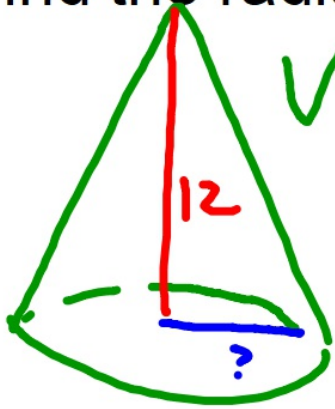


Cone S.A. $\pi r^2 + \pi r l$

A diagram illustrating the components of a cone's surface area. On the left, a small red circle represents the base of the cone. To its right, a red sector of a larger circle represents the lateral surface of the cone. The radius of the base circle is r , and the radius of the sector is the slant height l .

More review:

Find the radius of a 12" tall cone with a volume of 144π in³.



$$V = 144\pi = \frac{1}{3}\pi r^2 h$$

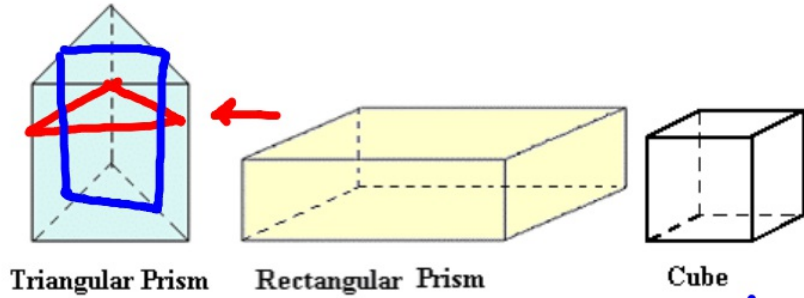
$$144 = \frac{1}{3}r^2 \cdot 12$$

$$144 = 4r^2$$

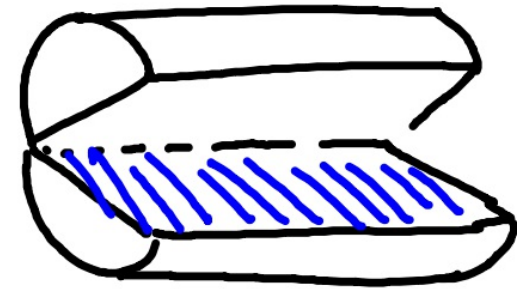
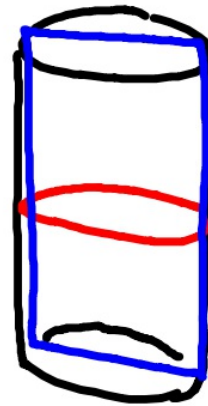
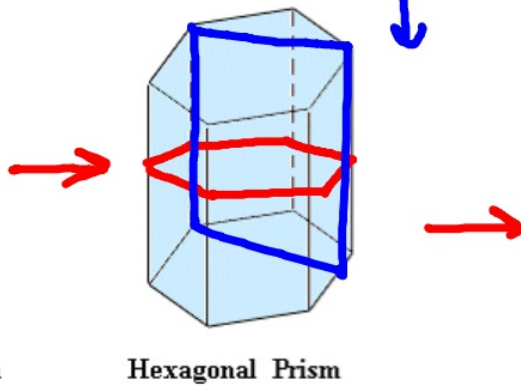
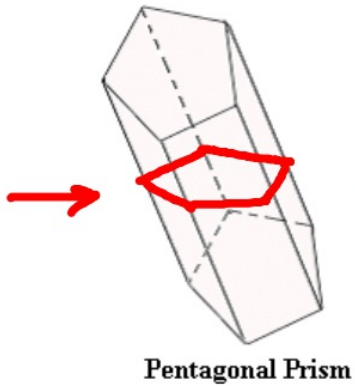
$$36 = r^2$$

$$6 = r$$

What are prisms?



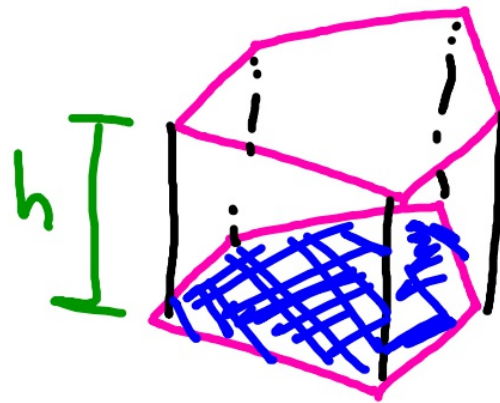
- an extrusion of a flat shape
- rectangular cross sections
- base shape cross sections



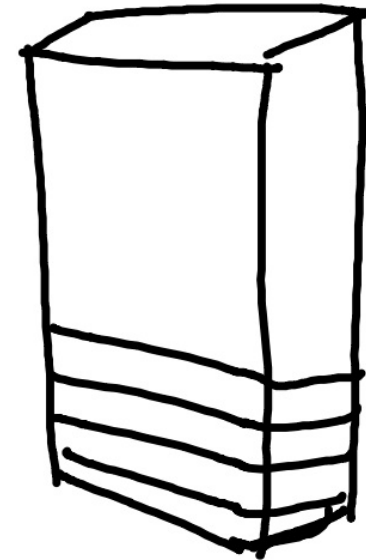
Prism Volume

$$V = Bh$$

B is base area



"club crackers"



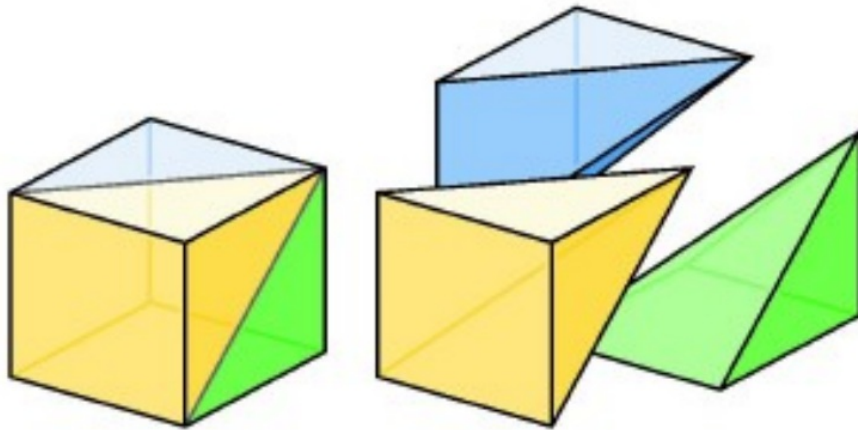
A prism is just a stack of
thin base-shape cross sections

ex: a cylinder is just a circle prism

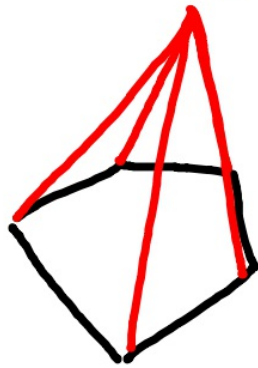
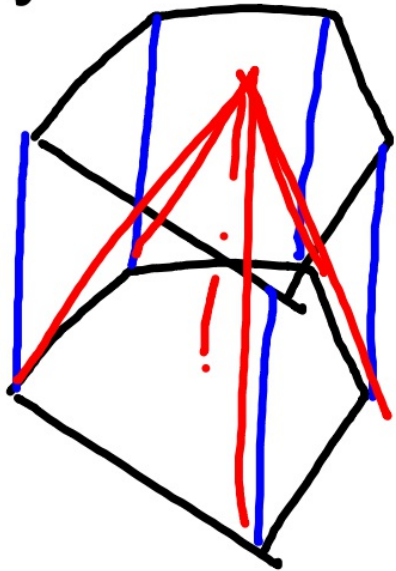


Rectangular Prism volume is very familiar: $V=lwh$

But what about pyramids?



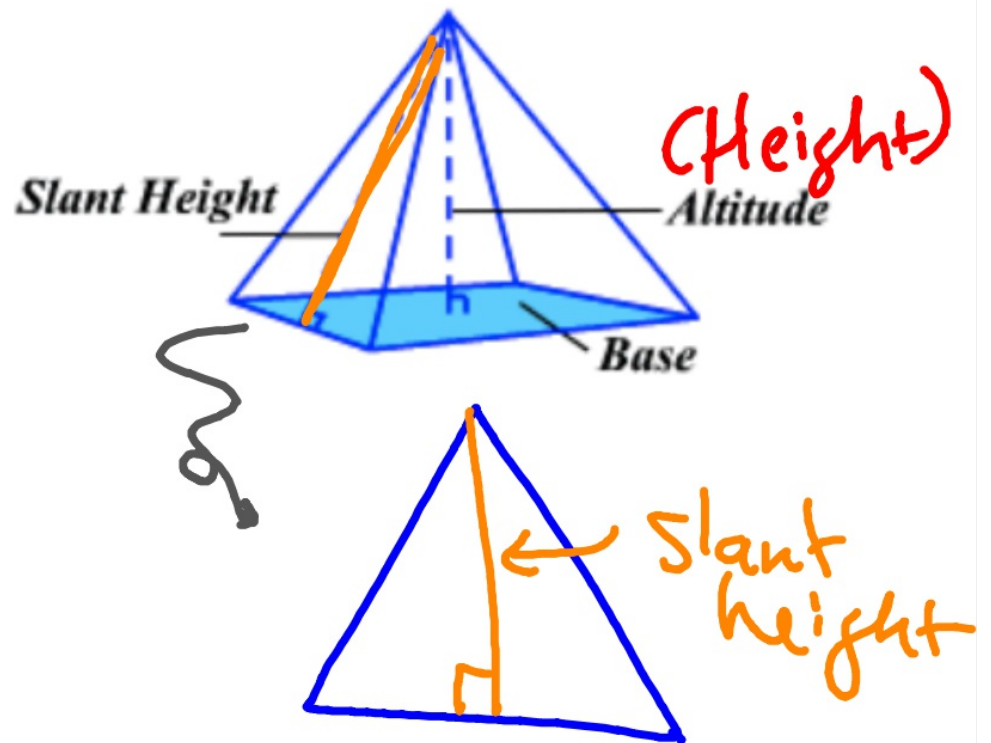
Cylinder: Cone :: Prism : Pyramid



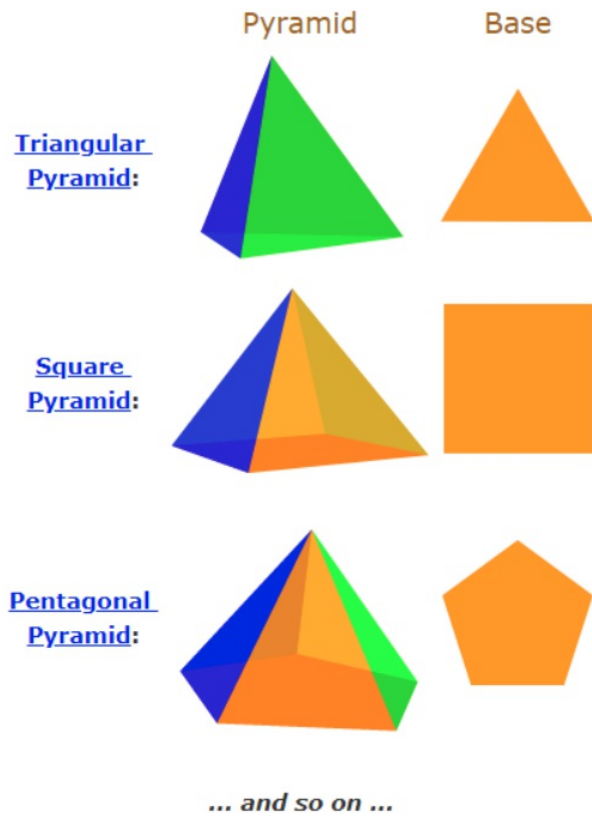
$$V_{\text{PYR}} = \frac{1}{3} B \cdot h$$

↑
Prism

takes 3 to fill Prism

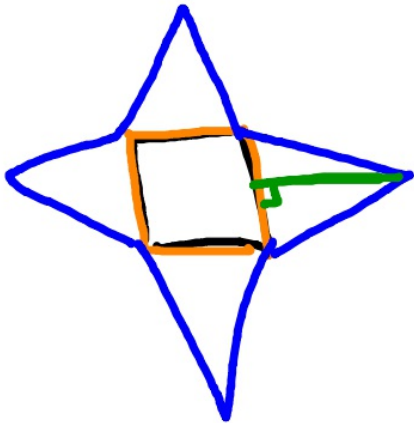
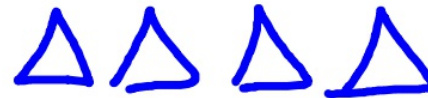
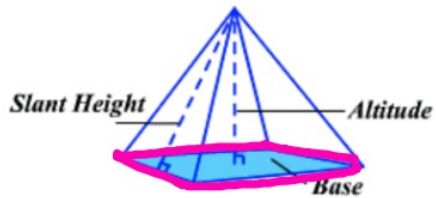


Any polygon can generate a prism or pyramid

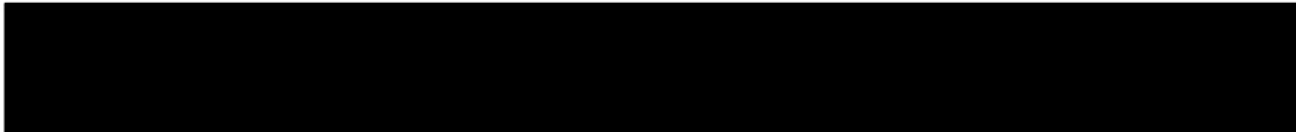


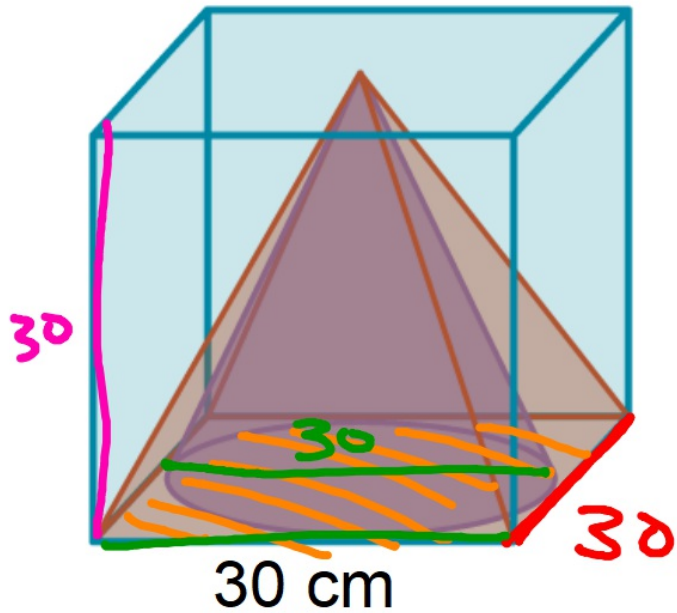
Pyramid Surface Area

$$SA = \text{base area} + \text{lateral area}$$



lateral area: $\frac{1}{2}(\text{slant})(\text{base perimeter})$





Cube with a nested pyramid and cone
 Find the volume of all 3 figures
 (2 dec.)

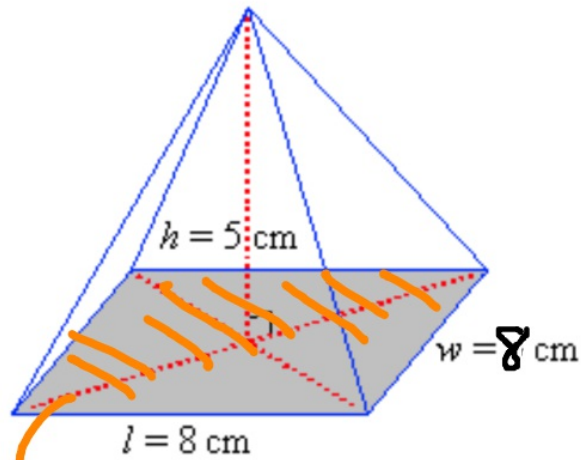
Cube: $V = B \cdot h$
 $(900)(30) = \boxed{27,000 \text{ cm}^3}$

Pyr: $\frac{1}{3} B \cdot h = \boxed{9,000 \text{ cm}^3}$

Cone: $\frac{1}{3} \pi (15)^2 \cdot 30$

$10\pi \cdot 15^2 = 2250\pi \approx \boxed{7068.58 \text{ cm}^3}$

Find the volume of this pyramid



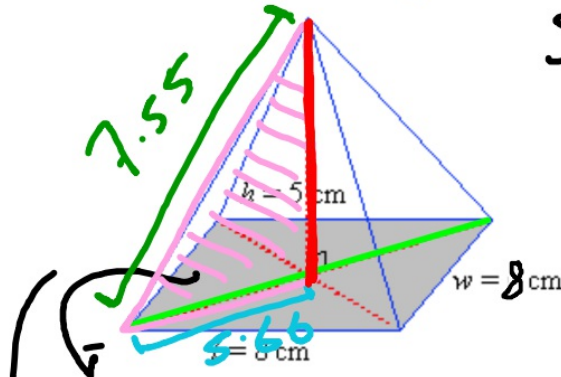
$$B = 64 \text{ cm}^2$$

$$V = \frac{1}{3} B \cdot h$$
$$= \frac{1}{3} (64) (5)$$

$$\approx 106.7 \text{ cm}^3$$

Now find its surface area

HINT: find the length of the green line

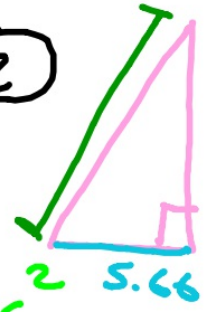


$$SA = B + LA$$

$$64 + \frac{1}{2}(\text{slant})(\text{base Perim})$$

32

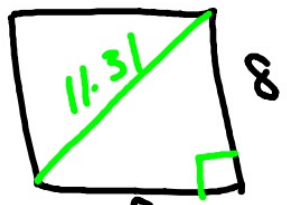
(2)



$$5^2 + 5.66^2 = c^2$$

$$7.55 = c$$

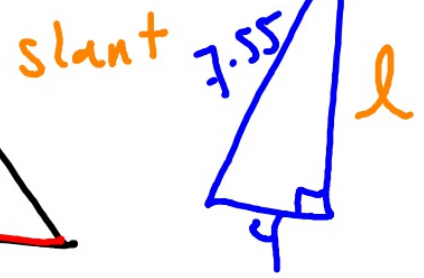
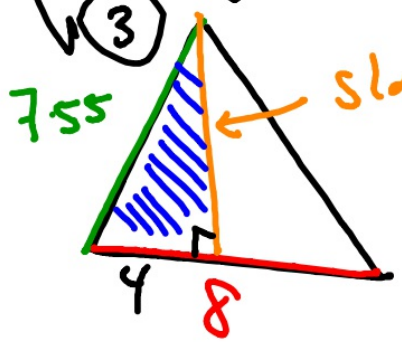
(1)



$$8^2 + 8^2 = c^2$$

$$11.31 = c$$

(3)



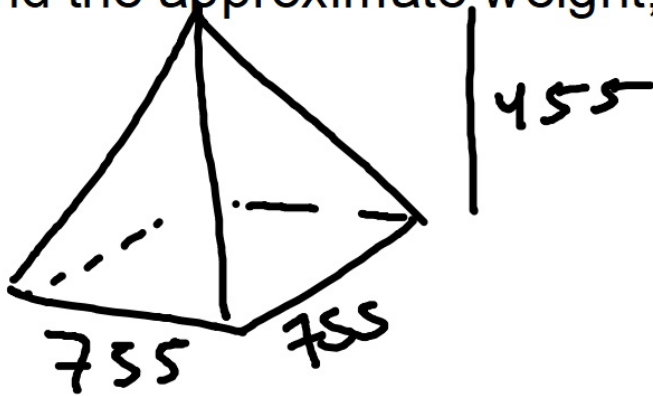
$$4^2 + 4^2 = 5.66^2$$

$$l = 6.40$$

$$SA = 64 + \frac{1}{2}(6.40)(32)$$

$$\approx 166.4 \text{ cm}^2$$

The Great Pyramid of Giza is a square pyramid with a base 755 feet long. It is 455 feet tall. If a cubic foot of limestone weighs 160 lbs, find the approximate weight, in tons, of the Pyramid. (1 ton = 2000 lbs)



$$V = \frac{1}{3} B h$$

$$V = \frac{1}{3} (755)(755)(455)$$

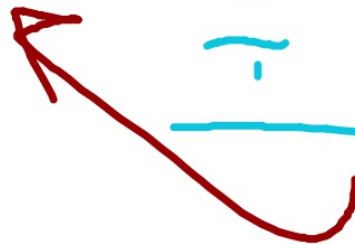
$$V = 8,645,379.67$$

6,916,303 tons

$$\times 160 \text{ lbs/ft}^3$$

$$1.38 \times 10^{10} \text{ lbs}$$

$$\div 2000 \text{ lbs/ton}$$



Practice Assessment

HW

finish the practice assessment, check solutions, review videos to help study for Thursday's test: mgeo.weebly.com