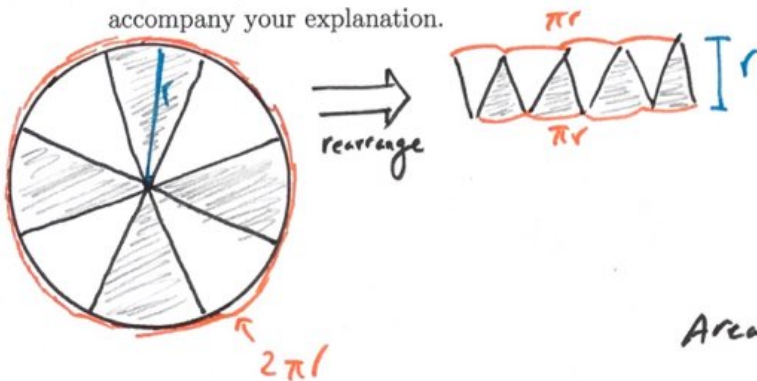


GMD-A1a

Practice Assessment Q4 #1

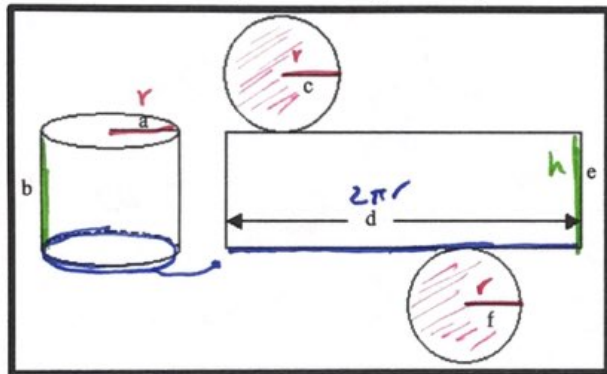
[NOTE: be ready to explain circumference, circle area, cylinder and/or cone surface area for real assessment]

1. Explain why the area of a circle with radius  $r$  can be found by  $A = \pi * r^2$ . You may use diagrams to accompany your explanation.



Rearrange slices of a circle into a 'rectangle'.  
 The base of the rectangle is half the circumference:  $\pi r$   
 The height of the 'rectangle' is the radius,  $r$   
 $Area = Base \cdot Height = \pi r \cdot r = \pi r^2$ . QED

2. Label each part correctly. Then give the full formula for cylinder surface area.



- a: radius,  $r$       b: height,  $h$       c: radius,  $r$   
 d: Circumference  $2\pi r$       e: height,  $h$       f: radius,  $r$

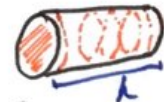
$SA = 2 \cdot \pi r^2 + 2\pi r h$

GMD-A1b

[NOTE: be ready to explain volume formulas for cylinders, cones, and prisms for this skill on real assessment.]

3. Explain why the volume of a cylinder can be found with  $V = \pi * r^2 * h$ . You may use diagrams to accompany your explanation.

A cylinder can be thought of as a stack of thin circles.  
 Each circle has area  $\pi r^2$ . The total 'height' of the stack is a representation of how many circles there are,  $h$ .



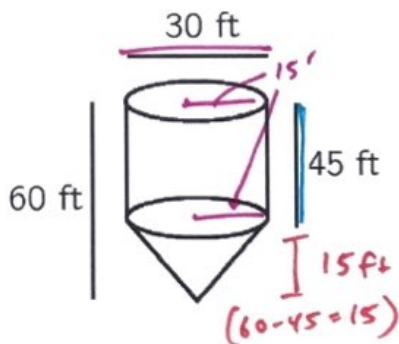
4. Explain why the volume of a cone with radius  $r$  and height  $h$  can be found by  $V = \frac{1}{3} * \pi * r^2 * h$ . You may use diagrams to accompany your explanation.

A cone with the same radius & height as a cylinder fills up only  $\frac{1}{3}$  as much space as the cylinder. Since the cylinder has volume  $\pi r^2 h$ , the cone is  $\frac{1}{3} \pi r^2 h$ .



GMD-A2a

5. A silo is being used to store excess grain. It is shaped as shown, including a cone. The structure is 60 feet tall in total, 30 feet wide at its base, and the cylindrical portion is 45 feet tall. To the nearest whole number, find the volume of the silo. Include units in your answer.



$$\text{Cylinder: } \pi r^2 \cdot h = \pi \cdot 15^2 \cdot 45 \approx 31,808.6 \text{ ft}^3$$

$$\text{Cone: } \frac{1}{3} \pi r^2 \cdot h = \frac{1}{3} \pi 15^2 \cdot 15 \approx 3534.3 \text{ ft}^3$$

$$\boxed{35,343 \text{ ft}^3}$$

6. Find the surface area of the exposed portions of the silo pictured above to the nearest whole number. Include units in your answer.

Cone Surface Area:

$$SA: \cancel{\pi r^2} + \pi r l$$



only the  $\pi r l$  part is exposed.



$$15^2 + 15^2 = l^2$$

$$225 + 225 = l^2$$

$$450 = l^2 \rightarrow l \approx 21.213$$

Cyl. Surface Area:

$$SA: 2\pi r^2 + 2\pi r h$$



only the rectangle and 1 circle are exposed.

$$\pi r l + 1 \cdot \pi r^2 + 2\pi r \cdot h$$

$$SA: \pi \cdot 15 \cdot 21.213 + \pi \cdot 15^2 + 2\pi (15)(45)$$

$$= 997.639 + 706.858 + 4271.15$$

$$= \boxed{5975.647 \text{ ft}^2}$$

7. Organizers are preparing water for an upcoming race. Each water cooler is a 2-foot tall cylinder with a

# #1 (Alt. method)

Subdivide circle into "rings". Longest/outer ring is the circumference,  $2\pi r$ .

"unravel" the rings into a triangle.



$2\pi r$

$$A = \frac{1}{2} b \cdot h$$

$$A = \frac{1}{2} \cdot 2\pi r \cdot r$$

$$A = \pi r \cdot r = \pi r^2$$

$2\pi r$

$$A = \frac{1}{2} \cdot b \cdot h$$

$$A = \frac{1}{2} \cdot 2\pi r \cdot r$$

$$A = \pi r^2$$

## Bonus Facts:

Why is  $\text{Vol}_{\text{cyl}} = \pi r^2 \cdot h$ ? A cylinder is a stack of circles. Each has area =  $\pi \cdot r^2$ . The infinitely thin "height" of each flat circle accumulates to give a total cylinder height equal to the height of the stack. So  $\pi r^2 \cdot h$  gives each circle's size times the "number" of circles.



## Why is $C = 2\pi r$ ?

$\pi$  is defined as  $\frac{\text{Circumference}}{\text{diameter}}$ . So  $\pi = \frac{C}{D}$   $D = 2r$  because 2 radii make a diameter. By substitution,  $\pi = \frac{C}{2r}$ . Multiply both sides by  $2r$  to give  $2\pi r = C$ .

SRT-C7a

7. If  $\sin(32) = z$  and  $\cos(\beta) = z$ , then what is the value of  $\beta$ ?

$\sin(32) = \cos(\beta)$

$32 + \beta = 90$

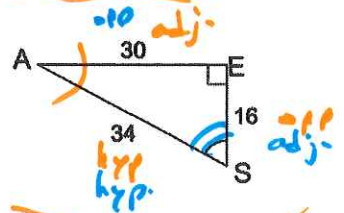
$\beta = 90 - 32 \Rightarrow \beta = 58^\circ$

Key Idea:  
If  $A + B = 90^\circ$  then  
 $\cos A = \sin B$   
 $\sin A = \cos B$

8. Write two trig ratios that both equal  $\frac{8}{17}$  based on the figure.

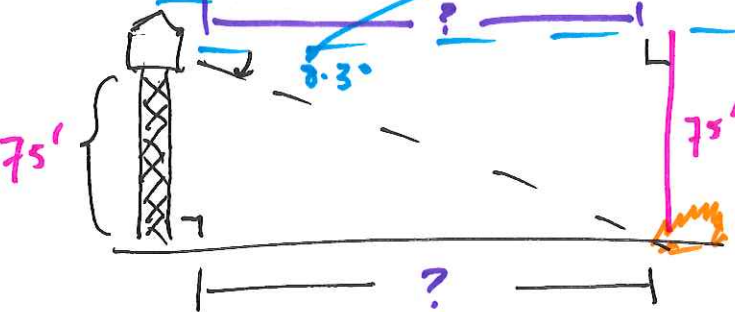
(Use the 2 acute angles)

$\sin A = \frac{\text{opp}}{\text{hyp}} = \frac{16}{34}$   
 $\cos S = \frac{\text{adj}}{\text{hyp}} = \frac{16}{34} (\div 2) \rightarrow \frac{8}{17}$



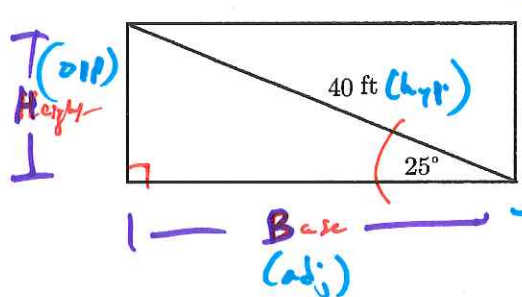
SRT-C8a:

9. A park ranger in a fire tower looks out of a 75-foot tall watchtower and spots a brush fire off in the distance. Using a clinometer, he measures the angle of depression of his line of sight down to the fire as  $8.3^\circ$ . How far to the nearest foot is the fire from the base of the watchtower?



Simplify  $\rightarrow$   $\tan(8.3^\circ) = \frac{75}{x}$   
 $x \cdot \tan(8.3^\circ) = 75$   
 $x = \frac{75}{\tan(8.3^\circ)} \rightarrow \approx 514 \text{ ft}$

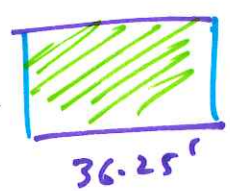
10. A rectangular field needs to be re-seeded for new grass. One bag of grass seed will cover 30 square feet. If each bag of grass seed costs \$15, find the amount of money remaining, if any, if the budget is \$800.



Need Area of Rectangle  $\rightarrow B \cdot H$

$\sin(25^\circ) = \frac{H}{40}$   
 $40 \cdot \sin 25 = h$   
 $16.9 \text{ ft} \approx h$

$\cos(25^\circ) = \frac{B}{40}$   
 $40 \cdot \cos 25 = B$   
 $36.25 \text{ ft} \approx B$



\$485 left over

AREA  $B \cdot H = (36.25)(16.9) = 612.625 \text{ sq ft.} \div 30 \text{ sq ft per bag} = 20.42 \text{ bags} \rightarrow \text{Need } 21$

Remainder?  
 $800 - 315 = \$485$